Wireless Magnetic-Based Closed-Loop Control of Self-Propelled Microjets

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Abstract

In this study, we demonstrate closed-loop motion control of self-propelled microjets under the influence of external magnetic fields. We control the orientation of the microjets using external magnetic torque, whereas the linear motion towards a reference position is accomplished by the thrust and pulling magnetic forces generated by the ejecting oxygen bubbles and field gradients, respectively. The magnetic dipole moment of the microjets is characterized using the U-turn technique, and its average is calculated to be $1.3 \times 10^{-12} \text{ A.m}^2$ at magnetic field and linear velocity of 2 mT and 100 μm/s, respectively. The characterized magnetic dipole moment is used in the realization of the magnetic force-current map of the microjets. This map in turn is used for the design of a closed-loop control system that does not depend on the exact dynamical model of the microjets and the accurate knowledge of the parameters of the magnetic system. The motion control characteristics in the transient- and steady-states depend on the concentration of the surrounding fluid (hydrogen peroxide solution) and the strength of the applied magnetic field. Our control system allows us to position microjets at an average velocity of 115 μm/s, and within an average region-of-convergence of 365 μm.

Introduction

Several types of catalytic [1–5] and magnetic [6,7] microrobots have been demonstrated to overcome Brownian motion at low-Reynolds number regimes [8,9]. Motion of these microrobots is based on several propulsion mechanisms. Some of these mechanisms depend on the efficient transformation of chemical energy into kinetic energy using catalytic reaction. Gibbs et al. [10] presented a model to explain the driving force for spherical colloids, and further showed that the propelling force depends on the surface tension of the liquid and the bulk concentration of hydrogen peroxide. Solovev et al. [11] and Mei et al. [12] have put forward a propulsion mechanism based on the catalytic decomposition of hydrogen peroxide by microtubular layers of platinum and silver, respectively. It has been also shown that self-propelled microjets can selectively transport relatively large amounts of particles on-a-chip and Murine Cath.a-differentiated cells by controlling the magnetic fields in open-loop [13]. Some propulsion mechanisms are based on pulling the magnetic microrobots with the magnetic field gradients [14–18]. However, these mechanisms are limited by the projection distance of the magnetic field gradients. Another propulsion mechanism was proposed by Bell et al. [19] and Sendoh et al. [20]. This mechanism mimics the morphology of the bacterial flagellum and capitalizes on the generation of rotating magnetic fields. The rotating fields allow the helical microrobot to rotate and act like a corkscrew [8], and hence moves without pulling by the magnetic field gradients.

Biological microrobots [21] have been used by Martel et al. to execute non-trivial tasks such as micro-manipulation [22], micro-assembly [23], and micro-actuation [24]. The propulsion mechanism of the biological microrobots depends on rotating their helical flagella to move forward or backward along the external magnetic field lines [25]. This propulsion mechanism allows biological microrobots to benefit from the larger projection distance of the magnetic field. However, the propulsion force of these microrobots is relatively small ($10^{-12}$ N) [26], and this decreases their range of applications. Wang et al. [27] has studied the use of both fuel-driven and fuel-free, as well as ultrasound-driven propulsion mechanisms at nano- and micro-scales. Although the previously mentioned propulsion mechanisms provide solutions to key challenges in microrobotic applications, progress towards practical implementation has not yet been accomplished. Substantial efforts have been dedicated to develop and characterize new propulsion mechanisms, whereas only a few attempts have been reported to realize practical applications based on closed-loop (feedback) control systems [28].

In this work, we demonstrate for the first time the closed-loop motion control of self-propelled microjets under the influence of controlled magnetic fields generated by a magnetic-based manipulation system. Figure 1 shows a control exerted over a microjet moving towards a reference position under the influence of the self-propulsion force and the applied magnetic fields. The ejecting oxygen bubbles provide thrust force which allows for the navigation of the microjet along the external magnetic field lines.
The experimental work of this study, hydrogen peroxide solution with concentration of 5% was used, along with small amounts of isopropanol and Triton X. A microjet with a length of 50 μm is immersed in the hydrogen peroxide. Uniform magnetic fields (field strength of 2 mT at the center of the electromagnetic array) are generated using two active electromagnetic coils at a time, and used to achieve a square trajectory of the microjet, as shown in Figure 2. Magnetic fields are measured using a calibrated three-axis Hall magnetometer (Sentron AG, Digital TeslaMeter 3MS1-A2D3-2-2T, Switzerland).

Characterization and Control Law

In order to position the self-propelled microjet within the vicinity of a reference point, a closed-loop motion control system is designed (Figure 3). The nominal equation of motion of the microjet is given by

$$F(P) + f(P,t) + F_d(P) = 0,$$

where $F(P)$, $f(P,t)$, and $F_d(P)$ are the magnetic force, self-propulsion force, and drag force of the microjet at point $P$, respectively. Our motion control strategy is based on controlling the magnetic force ($F(P)$) towards a reference position. This control allows the field lines to be directed towards the reference position. A microjet aligns itself along the field lines and moves towards the reference position using its self-propulsion force. The magnetic force is generated using an external magnetic field ($B(P)$), and is given by [16,26]

$$F(P) = (m \cdot V)B(P) = (m \cdot V)B(P)I = A(m,P)I,$$

where $B(P)$ is a matrix that maps the input current ($I$) onto magnetic field ($B(P)$). Further, $A(m,P)$ maps the input current

Figure 1. Closed-loop motion control of a self-propelled microjet under the influence of the controlled magnetic fields. Magnetic fields are generated using the magnetic-based manipulation system, shown in the inset at the bottom left corner [14]. The magnetic fields are used to orient the microjet towards the reference position (black circle). The microjet moves towards the reference position using the thrust force generated by the ejecting oxygen bubbles from its end. The velocity of the microjet in this representative experiment is 100 μm/s for hydrogen peroxide solution with concentration of 5%. The inset at the upper right corner shows a Scanning Electron Microscopy image of a microjet fixed to its substrate.

doi:10.1371/journal.pone.0083053.g001
onto magnetic force. This force-current map depends on the magnetic dipole moment \(m\) of the microjet and its position \(P\). We estimate the magnetic dipole moment of the microjets to realize the magnetic force-current map \((2)\). A microjet aligns itself along the magnetic field lines. Reversing the direction of the magnetic fields causes the microjet to follow a \(U\)-turn trajectory, as shown in Figure 4. The diameter \(D\) of the \(U\)-turn trajectory is given by \([30,31]\)

\[
D = \frac{x \pi |P|}{|m| |B(P)|},
\]

where \(x\) is the rotational drag coefficient of the microjet, and \(\dot{P}\) is its linear velocity. In order to determine the magnetic dipole moment of the microjet using \((3)\), uniform magnetic fields are applied using electromagnets A and C (Figure 1). These fields are reversed to initiate \(U\)-turns of the microjets. We repeated this experiment 10 times and the average \(U\)-turn diameter is determined from the motion analysis of the microjets. The average magnetic dipole moment is calculated to be \(1.31 \times 10^{-12} \text{A.m}^2\), at magnetic field and linear velocity of 2 mT and 100 \(\mu\text{m/s}\), respectively. In \((3)\), \(x\) is calculated using \([33]\)

\[
x = \frac{\pi \eta l^3}{3} \left[ \ln \left(\frac{l}{d}\right) + 0.92 \left(\frac{d}{l}\right) - 0.662 \right]^{-1},
\]

where \(\eta\) is the dynamic viscosity of the hydrogen peroxide solution. Further, \(l\) and \(d\) are the length (50 \(\mu\text{m}\)) and diameter (5 \(\mu\text{m}\)) of the microjet, respectively.

The magnetic dipole moment is used in the realization of the magnetic force current map \((2)\), this map is a basis of magnetic-based closed-loop control systems. First, we devise the following sliding-mode control input \([29]\):

\[
F(P) = -\dot{r}(P,t) - 2x|\dot{P}|\dot{P} - x|\dot{I}|\Gamma(P),
\]

Figure 2. Open-loop motion control of a self-propelled microjet using uniform magnetic fields. The microjet follows a square trajectory with an edge length of 500 \(\mu\text{m}\), at a linear velocity of 100 \(\mu\text{m/s}\). Uniform magnetic fields are generated using 2 active electromagnets at a time. The bottom row provides finite element (FE) simulations of the uniform magnetic fields utilized in this open-loop control experiment. \(I_i\) for \((i = 1, \ldots, 4)\), denotes the current at each of the electromagnets. The magnetic field strength within the center of the workspace is 2 mT. The black arrows point at the microjet.

doi:10.1371/journal.pone.0083053.g002

Figure 3. Closed-loop control system for precise positioning of self-propelled microjets (inset). \(P\) and \(P_{\text{ref}}\) denote the position of the microjet and the reference position, respectively, and \(I\) denotes the current vector.

doi:10.1371/journal.pone.0083053.g003
where $\hat{f}(P,t)$ is an estimate of the propulsion force given in (1). Further, $P_{\text{ref}}$ is the reference velocity, and $\Gamma(P)$ is an additional force input and is given by

$$\Gamma(P) = \frac{1}{2} \left(-\Sigma(P,t) - \beta\right) \text{sgn}(s(t)).$$

(6)

In (6), $s(t)$ is the sliding-line and is given by

$$s(t) = \dot{e} + \lambda e = 0,$$

(7)

where $e$ and $\dot{e}$ are the position and velocity tracking errors, respectively. Further, $\beta$ and $\lambda$ are positive gains. Finally, $\sum (P,t)$ is given by

$$\sum (P,t) = \frac{1}{2\eta} \left(\hat{f}(P,t) - f(P,t)\right).$$

(8)

### Motion Control Results

The sliding-mode control law (5) is implemented by setting (5) equal to (2), and solving for the current vector ($I$) using the pseudoinverse of $L(m,P)$. Figure 5 shows a representative closed-loop motion control result of the control law (5). The position error is determined by tracking the motion of the microjet (large blue circle in Figure 5). This position tracking error along with its time derivative are used to calculate $s(t)$. Further, the self-propulsion force estimate ($\hat{f}(P,t)$) is modeled using a periodic force function with a period of 0.08 second. This period is determined from the motion analysis of the microjets. This time is based on the average
elapsed-time of the ejecting oxygen bubbles. Control law (5) allows the magnetic field to orient towards the reference positions (small blue circle). The microjet moves towards the reference position at an average velocity of 90 $\text{m/s}$. Due to the self-propulsion force of the microjet, our control system cannot achieve zero position tracking error. It rather positions the microjet within the vicinity of the reference position, which we refer to as a region-of-convergence as shown in Figure 6.

Figure 6 shows the controlled motion of a microjet towards three reference positions. Within the vicinity of the reference position, the control system reverses the direction of the magnetic field based on the position and velocity tracking errors (7). This magnetic field reversal allows the microjet to stay within the vicinity of the reference position. Diameter of this region-of-convergence depends on the linear velocity of the microjet, the magnetic torque exerted on its magnetic layers, and the bandwidth of the control system (our microscopic vision system has a maximum frame-per-second of 15). The sliding-mode control gains ($\lambda$ and $\beta$) must be positive. The gain $\lambda$ controls the slope of the sliding-line (7), whereas the gain $\beta$ controls the convergence time of the errors ($\epsilon$ and $\dot{\epsilon}$) to the sliding-line. In this representative experiment (Figure 6), we observe that setting the controller gains to $\lambda = 12$ and $\beta = 1.3$, results in an average velocity of 97 $\mu\text{m/s}$ and maximum region-of-convergence of 524 $\mu\text{m}$. This motion control trail is repeated 10 times, and the average velocity and average region-of-convergence are calculated to be $115 \pm 26 \mu\text{m/s}$ and $356 \pm 110 \mu\text{m}$, respectively.

In order to evaluate the characteristics of the sliding-mode control system, we compare its results to a conventional PD control system. In this case, the magnetic force is given by

$$F(P) = K_P \epsilon + K_D \dot{\epsilon}.$$  \hfill (9) 

where $K_P$ and $K_D$ are the controller positive-definite gain matrices. Control law (9) is implemented by setting the PD control force equal to the magnetic force-current map (2), and calculating the current vector using the pseudoinverse of $\Lambda(m,P)$ that is based on the characterized magnetic dipole moment and position of the microjet. We observe that the PD control system achieves an average velocity and region-of-convergence of $119 \pm 30 \mu\text{m/s}$ and $417 \pm 115 \mu\text{m}$, respectively. The averages are calculated from 10 closed-loop motion control trials. Figure 7 shows a representative

![Figure 6](image_url)

**Figure 6.** Representative closed-loop control of a self-propelled microjet under the influence of the controlled magnetic fields, using the sliding-mode control law (5). (a) The sliding-mode control system positions the microjet at an average velocity of 97 $\mu\text{m/s}$, and within a maximum region-of-convergence (ROC) of 524 $\mu\text{m}$ in diameter. ROCs are represented using the red-dashed circles. The controller gains are: $\lambda = 12$ and $\beta = 1.3$. The red arrows indicate the direction of the microjet, whereas the blue arrows indicate the reference positions. (b) Motion of the microjet towards three reference positions (blue vertical lines) along $x$-axis. (c) Motion of the microjet along $y$-axis.

doi:10.1371/journal.pone.0083053.g006

![Figure 7](image_url)

**Figure 7.** Representative closed-loop control of a self-propelled microjet under the influence of the controlled magnetic fields, using the proportional-derivative (PD) control law (9). (a) The PD control system positions the microjet at an average velocity of 127 $\mu\text{m/s}$, and within a maximum region-of-convergence (ROC) of 662 $\mu\text{m}$ in diameter. ROCs are represented using the red-dashed circles. The controller gains are: $k_{p1} = k_{p2} = 15$ and $k_{d1} = k_{d2} = 5$, where ($k_{pi}$) and ($k_{di}$) are the entries of the gain matrices ($K_P$) and ($K_D$) for ($i = 1, 2$), respectively. The red arrows indicate the direction of the microjet, whereas the blue arrows indicate the reference positions. (b) Motion of the microjet towards three reference positions (blue vertical lines) along $x$-axis. (c) Motion of the microjet along $y$-axis.

doi:10.1371/journal.pone.0083053.g007
motion control result of the microjet using the PD control system. These results show that the non-linear sliding-mode control system achieves 14% higher positioning accuracy, as opposed to the linear PD control system, in the steady-state.

Conclusions
Closed-loop control of self-propelled microjets is implemented using a magnetic-based manipulation system and a sliding-mode controller. Magnetic fields are generated and oriented based on the position tracking error of the microjet with respect to the reference position. This control allows the microjet to orient along the field lines using the magnetic torque exerted on its iron layers. The magnetic torque is calculated to be 2.6 × 10⁻¹³ N.m, based on the characterized magnetic dipole moment of the microjet and the maximum magnetic fields (2 mT) used throughout the experimental work. This magnetic torque allows the microjet to overcome a drag torque of 3.3 × 10⁻¹⁰ N.m, based on an angular velocity of 25 rad/sec. Our control system uses the magnetic torque only to keep the microjet within the vicinity of the reference position due to the self-propulsion force of the microjet that cannot be controlled during a motion control task. The unmodeled dynamics due to the wall and surface effects and microjet-bubbles interactions are mitigated using a sliding-mode control system. This control system achieves 14% higher positioning accuracy than a magnetic-based PD control system. The accuracy provided by the proposed closed-control system could allow microjets to be used in micro-manipulation, micro-assembly, micro-actuation, and applications that are not yet conceived.

Author Contributions
Conceived and designed the experiments: ISMK VM SS SM. Performed the experiments: ISMK. Analyzed the data: ISMK SS OGS SM. Contributed reagents/materials/analysis tools: ISMK SS OGS SM. Wrote the paper: ISMK.

References